Package 'semicontMANOVA'

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Title Multivariate ANalysis of VAriance with Ridge Regularization for Semicontinuous High-Dimensional Data
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Description Implements Multivariate ANalysis Of VAriance (MANOVA) parameters' inference and test with regularization for semicontinuous high-dimensional data. The method can be applied also in presence of low-dimensional data. The p-value can be obtained through asymptotic distribution or using a permutation procedure. The package gives also the possibility to simulate this type of data. Method is described in Elena Sabbioni, Claudio Agostinelli and Alessio Farcomeni (2024) <arxiv:2401.04036>.</arxiv:2401.04036>
License GPL-2
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R topics documented:
scMANOVA2scMANOVAestimation4scMANOVApermTest6scMANOVAsimulation8
Index 10

2 scMANOVA

scMANOVA	Multivariate ANalysis Of VAriance Inference and Test with Ridge Reg-
	ularization for Semicontinuous High-Dimensional Data

Description

scMANOVA performs Multivariate ANalysis Of VAriance (MANOVA) inference and test with ridge regularization in presence of semicontinuous high-dimensional data. The test is based on a Likelihood Ratio Test statistic and the p-value can be computed using either asymptotic distribution (p.value.perm = FALSE) or via permutation procedure (p.value.perm = TRUE). There is the possibility to provide as input the regularization parameters or to choose them through an optimization procedure.

Usage

```
scMANOVA(x, n, lambda = NULL, lambda0 = NULL, lambda.step = 0.1,
ident = FALSE, tol = 1e-08, penalty = function(n, p) log(n),
B = 500, p.value.perm = FALSE, fixed.lambda = FALSE, ...)
```

Arguments

X	$\mbox{\tt data.frame}$ or $\mbox{\tt matrix}$ of data with units on the rows and variables on the columns
n	vector. The length corresponds to the number of groups, the elements to the number of observations in each group
lambda	NULL, a scalar or a vector of length 2. Ridge regularization parameter. The optimal value of lambda is searched in the interval [0,100] if NULL, and in the specified interval when it is a vector of length 2, otherwise it is used as the optimal value
lambda0	NULL, a scalar or a vector of length 2. Ridge regularization parameter under null hypothesis. The optimal value of lambda0 is searched in the interval [0,100] if NULL, and in the specified interval when it is a vector of length 2, otherwise it is used as the optimal value
lambda.step	scalar. Step size used in the optimization procedure to find the smallest value of lambda (and lambda0) that makes the covariance matrices, under the alternative and under the null hypotheses, non singular
ident	logical. If TRUE, lambda times the identity matrix is added to the raw estimated covariance matrix, if FALSE the diagonal values of the raw estimated covariance matrix are used instead
tol	scalar. Used in the optimization procedure to find the smallest value of lambda (and lambda0) that makes the covariance matrices, under the alternative and under the null, non singular
penalty	function with two arguments: sample size (n) and number of variables (p) used as penalty function in the definition of the Information Criterion to select the optimal values for lambda and lambda0

scMANOVA 3

B scalar. Number of permutations to run in the permutation test

p.value.perm logical. If TRUE a p-value from a permutation test is evaluated, otherwise an

asymptotic value is reported

fixed.lambda logical. If TRUE the optimal values for lambda and lambda@ are evaluated

just once for the observed dataset and kept fixed during the permutation test,

otherwise, optimal values are evaluated for each permuted datsets

... further parameters passed to function scMANOVApermTest

Value

An object of class scMANOVA which is a list with the following components

pi matrix. Estimated proportion of missing values for each group

mu matrix. Estimated mean vector for each group

sigmaRidge matrix. Estimated covariance matrix with ridge regularization sigma matrix. Estimated covariance matrix by maximum likelihood

pi0 vector. Estimated proportion of missing values under the null hypothesis

mu0 vector. Estimated mean vector under the null hypothesis

sigma@Ridge matrix. Estimated covariance matrix with ridge regularization under null hy-

pothesis

sigma0 matrix. Estimated covariance matrix by maximum likelihood under null hy-

pothesis

removed.vars vector or NULL. columns removed in the continuous part of the log-likelihood

dues to insufficient number of observations in each group

logLikPi scalar. Log-likelihood for the discrete part of the model

logLik scalar. Log-likelihood

logLikPi0 scalar. Log-likelihood for the discrete part of the model under the null hypothe-

SIS

logLik0 scalar. Log-likelihood under null hypothesis

statistic scalar. Wilks statistics

lambda scalar. Regularization parameter

lambda0 scalar. Regularization parameter under null hypothesis

df scalar. Model degree of freedom

df0 scalar. Model degree of freedom under null hypothesis

aic scalar. Information criteria

aic0 scalar. Information criteria under null hypothesis

p. value scalar. p-value of the Wilks statistic

Author(s)

Elena Sabbioni, Claudio Agostinelli and Alessio Farcomeni

4 scMANOVAestimation

References

Elena Sabbioni, Claudio Agostinelli and Alessio Farcomeni (2024) A regularized MANOVA test for semicontinuous high-dimensional data. arXiv: http://arxiv.org/abs/2401.04036

See Also

scMANOVAestimation and scMANOVApermTest

Examples

```
set.seed(1234) \\ n <- c(5,5) \\ p <- 20 \\ pmiss <- 0.1 \\ x <- scMANOVAsimulation(n=n, p=p, pmiss=pmiss) \\ res.asy <- scMANOVA(x=x, n=n) \# Asymptotic p.value \\ res.asy \\ res.perm <- scMANOVA(x=x, n=n, p.value.perm=TRUE) \# p-value by permutation test \\ res.perm \\ \end{tabular}
```

scMANOVAestimation

Multivariate ANalysis Of VAriance Maximum Likelihood Estimation with Ridge Regularization for Semicontinuous High-Dimensional Data

Description

scMANOVAestimation computes the regularized Multivariate ANalysis Of VAriance (MANOVA) maximum likelihood estimates for semicontinuous high-dimensional data. The estimation can be performed also for low-dimensional data. The regularization parameters are provided as input and the user can decide to perform the regularization adding the identity matrix to the raw estimated covariance matrix (default, ident=TRUE) or adding the diagonal values of the raw estimated covariance matrix (ident=FALSE).

Usage

```
scMANOVAestimation(x, n, lambda = NULL, lambda0 = NULL,
ident = TRUE, posdef.check = TRUE, rm.vars = NA)
```

Arguments

X	data.frame or matrix of data with units on the rows and variables on the columns
n	vector. The length corresponds to the number of groups, the elements to the number of observations in each group
lambda	scalar. Ridge regularization parameter

scMANOVAestimation 5

lambda0 scalar. Ridge regularization parameter under null hypothesis

ident logical. If TRUE, lambda times the identity matrix is added to the raw estimated

covariance matrix, if FALSE the diagonal values of the raw estimated covariance

matrix are used instead

posdef.check logical. Check if the estimated covariance matrix is positive definite

rm. vars NA, NULL or vector. If NA variables are removed from the analysis when they do

not have enough observations to compute covariances. If NULL or a zero length vector all the variables are retained. If it is a vector, it indicates the position

of the variables to remove, no further variables are removed

Value

An object of class scMANOVA estimation which is a list with the following components

pi matrix. Estimated proportion of missing values for each group

mu matrix. Estimated mean vector for each group

sigmaRidge matrix. Estimated covariance matrix with ridge regularization sigma matrix. Estimated covariance matrix by maximum likelihood

pi0 vector. Estimated proportion of missing values under the null hypothesis

mu0 vector. Estimated mean vector under the null hypothesis

sigma@Ridge matrix. Estimated covariance matrix with ridge regularization under null hy-

pothesis

sigma0 matrix. Estimated covariance matrix by maximum likelihood under null hy-

pothesis

removed.vars vector or NULL. columns removed in the continuous part of the log-likelihood

dues to insufficient number of observations in each group

logLikPi scalar. Log-likelihood for the discrete part of the model

logLik scalar. Log-likelihood

logLikPi0 scalar. Log-likelihood for the discrete part of the model under the null hypothe-

SIS

logLik0 scalar. Log-likelihood under null hypothesis

Author(s)

Elena Sabbioni, Claudio Agostinelli and Alessio Farcomeni

References

Elena Sabbioni, Claudio Agostinelli and Alessio Farcomeni (2024) A regularized MANOVA test for semicontinuous high-dimensional data. arXiv: http://arxiv.org/abs/2401.04036

See Also

scMANOVA and scMANOVApermTest

Examples

```
set.seed(1234)
n <- c(5,5)
p <- 20
pmiss <- 0.1
x <- scMANOVAsimulation(n=n, p=p, pmiss=pmiss)
res <- scMANOVAestimation(x=x, n=n, lambda=3.59, lambda0=3.13)
res</pre>
```

scMANOVApermTest

Multivariate ANalysis Of VAriance log-likelihood Test with Ridge Regularization for Semicontinuous High-Dimensional Data

Description

scMANOVApermTest uses a permutation procedure to perform a test based on a Multivariate ANalysis Of VAriance(MANOVA) Likelihood Ratio test statistic with a ridge regularization. The statistic is developed for semicontinuous and high-dimensional data, but can be used also in low-dimensional scenarios.

Usage

```
scMANOVApermTest(x, n, lambda = NULL, lambda0 = NULL, lambda.step = 0.1,
ident = FALSE, tol = 1e-08, penalty = function(n, p) log(n), B = 500,
parallel = c("no", "multicore", "snow"), ncpus = 1L, cl = NULL,
only.pvalue = TRUE, rm.vars = NA, ...)
```

Arguments

x	$\mbox{\tt data.frame}$ or $\mbox{\tt matrix}$ of data with units on the rows and variables on the columns
n	vector. The length corresponds to the number of groups, the elements to the number of observations in each group
lambda	scalar or a vector of length 2. Ridge regularization parameter. The optimal value of lambda is searched in the specified interval when it is a vector of length 2, otherwise it is used as the optimal value
lambda0	NULL, a scalar or a vector of length 2. Ridge regularization parameter under null hypothesis. The optimal value of lambda0 is searched in the specified interval when it is a vector of length 2, otherwise it is used as the optimal value
lambda.step	scalar. Step size used in the optimization procedure to find the smallest value of lambda (and lambda0) that makes the covariance matrices, under the alternative and under the null hypothesis, non singular
ident	logical. If TRUE, lambda times the identity matrix is added to the raw estimated covariance matrix, if FALSE the diagonal values of the raw estimated covariance matrix are used instead

scMANOVApermTest 7

tol	scalar. Used in the optimization procedure to find the smallest value of lambda (and lambda0) that makes the covariance matrices, under the alternative and under the null hypothesis, non singular
penalty	function with two arguments: sample size (n) and number of variables (p) used as penalty function in the definition of the Information Criterion to select the optimal values for lambda and lambda0
В	scalar. Number of permutations to run in the permutation test
parallel	The type of parallel operation to be used (if any)
ncpus	integer. Number of processes to be used in parallel operation: typically one would chose this to the number of available CPUs.
cl	An optional parallel or snow cluster to use if parallel = "snow". If not supplied, a cluster on the local machine is created for the duration of the call
only.pvalue	logical. If TRUE only the p-value is returned
rm.vars	vector. It indicates the position of the variables to remove
	Further parameters passed to parallel::mclapply in case of parallel="multicore"

Value

If only.pvalue=TRUE (default) a scalar which is the p-value of the Wilks statistic obtain by a permutation procedure, otherwise an object of class htest

Author(s)

Elena Sabbioni, Claudio Agostinelli and Alessio Farcomeni

References

Elena Sabbioni, Claudio Agostinelli and Alessio Farcomeni (2024) A regularized MANOVA test for semicontinuous high-dimensional data. arXiv: http://arxiv.org/abs/2401.04036

See Also

scMANOVA and scMANOVAestimation

Examples

```
set.seed(1234)
n <- c(5,5)
p <- 20
pmiss <- 0.1
x <- scMANOVAsimulation(n=n, p=p, pmiss=pmiss)
res <- scMANOVApermTest(x=x, n=n, lambda=3.59, lambda0=3.13,
    only.pvalue=FALSE)
res</pre>
```

8 scMANOVA simulation

scMANOVAsimulation	Simulation of datasets for a	semicontinuous scenarios
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Description

Simulation of dataset of semicontinuous data coming from different groups, with specific marginal probabilities of a missing value, specific mean vectors and common covariance matrix.

Usage

```
scMANOVAsimulation(n, p, pmiss = 0, rho = 0, mu = NULL,
    sigma = NULL, only.data = TRUE)
```

Arguments

n	vector. The length corresponds to the number of groups, the elements to the number of observations in each group
р	scalar. Number of variables (columns)
pmiss	scalar or vector. Proportion of missingness in each group. If it is a scalar the same proportion is used in each group
rho	scalar. If $sigma=NULL$ then $sigma$ is set as a covariance matrix with covariance rho equal in every entries that is not on the main diagonal of $sigma$, and variance equal to 1
mu	NULL or vector or matrix. If NULL the mean of each group is set zero for all the variables, if vector the different groups have the same mean. If matrix each row corresponds to the mean vector of the corresponding group
sigma	$\mbox{\scriptsize NULL}$ or matrix. If matrix it is a covariance matrix. If $\mbox{\scriptsize NULL}$ the value of rho is used to build the covariance matrix
only.data	logical. If TRUE only the simulated data are reported

Value

pmiss

If only.data=TRUE an object of class matrix is reported otherwise a list with the following components

х	matrix. The simulated dataset
У	$\mbox{\tt matrix}.$ A matrix with zero when the corresponding entry in x is zero and one otherwise
original	matrix. The simulated dataset without missing values
mu	matrix. Mean vectors, on for each group
sigma	matrix. Covariance matric
n	As in input
p	As in input

vector. Proportion of missingness in each group

scMANOVAsimulation 9

Author(s)

Elena Sabbioni, Claudio Agostinelli and Alessio Farcomeni

References

Elena Sabbioni, Claudio Agostinelli and Alessio Farcomeni (2024) A regularized MANOVA test for semicontinuous high-dimensional data. arXiv: http://arxiv.org/abs/2401.04036

See Also

 $scMANOVA estimation \ and \ scMANOVA permTest$

Examples

```
set.seed(1234)

n \leftarrow c(5,5)

p \leftarrow 20

pmiss \leftarrow 0.1

x \leftarrow scMANOVAsimulation(n=n, p=p, pmiss=pmiss)
```

Index

```
* datasets
    scMANOVAsimulation, 8
* htest
    scMANOVA, 2
    scMANOVApermTest, 6
* manova
    scMANOVA, 2
    scMANOVAestimation, 4
    scMANOVApermTest, 6
    scMANOVAsimulation, 8
* multivariate
    scMANOVA, 2
    scMANOVAestimation, 4
    scMANOVApermTest, 6
    scMANOVAsimulation, 8
* permutation
    scMANOVA, 2
    scMANOVApermTest, 6
* regression
    scMANOVA, 2
    scMANOVAestimation, 4
    scMANOVApermTest, 6
* regularization
    scMANOVA, 2
    scMANOVAestimation, 4
    scMANOVApermTest, 6
* ridge
    scMANOVA, 2
    scMANOVAestimation, 4
    scMANOVApermTest, 6
scMANOVA, 2, 5, 7
scMANOVAestimation, 4, 4, 7, 9
scMANOVApermTest, 3-5, 6, 9
scMANOVAsimulation, 8
```