Package 'Zseq'

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Zseq-package

Zseq: Integer Sequence Generator

Description

The world of integer sequence has long history, which has been accumulated in The On-Line Encyclopedia of Integer Sequences. Even though R is not a first pick for many number theorists, we introduce our package to enrich the R ecosystem as well as provide pedagogical toolset. We adopted **gmp** for flexible large number computations in that users can easily experience large number sequences on a non-exclusive generic computing platform.

Abundant 3

Abundant

Abundant numbers

Description

Under OEIS A005101, an *abundant* number is a number whose proper divisors sum up to the extent greater than the number itself. First 6 abundant numbers are 12, 18, 20, 24, 30, 36.

Usage

```
Abundant(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

```
Deficient, Perfect
```

Examples

```
## generate first 30 Abundant numbers and print it
print(Abundant(30))
```

Achilles

Achilles numbers

Description

Under OEIS A052486, an *Achilles* number is a number that is *powerful* but *not perfect*. First 6 Achilles numbers are 72, 108, 200, 288, 392, 432.

Usage

```
Achilles(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

4 Bell

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 3 Achilles numbers and print
print(Achilles(3))
```

Bell

Bell numbers

Description

Under OEIS A000110, the *n*th *Bell* number is the number of ways to partition a set of n labeled elements, where the first 6 entries are 1, 1, 2, 5, 15, 52.

Usage

```
Bell(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

```
## generate first 30 Bell numbers and print
print(Bell(30))
```

Carmichael 5

Carmichael

Carmichael numbers

Description

Under OEIS A002997, a Carmichael number is a composite number n such that

$$b^{n-1} = 1(modn)$$

for all integers b which are relatively prime to n. First 6 Carmichael numbers are 561, 1105, 1729, 2465, 2821, 6601.

Usage

```
Carmichael(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 3 Carmichael numbers
print(Carmichael(3))
```

Catalan

Catalan numbers

Description

Under OEIS A000108, the nth Catalan number is given as

$$C_n = \frac{(2n)!}{(n+1)!n!}$$

where the first 6 entries are 1, 1, 2, 5, 14, 42 with $n \ge 0$.

```
Catalan(n, gmp = TRUE)
```

6 Composite

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 30 Catalan numbers
print(Catalan(30))
```

Composite

Composite numbers

Description

Under OEIS A002808, a *composite* number is a positive integer that can be represented as multiplication of two smaller positive integers. The first 6 composite numbers are 4, 6, 8, 9, 10, 12.

Usage

```
Composite(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

```
## generate first 30 Composite numbers
print(Composite(30))
```

Deficient 7

Deficient

Deficient numbers

Description

Under OEIS A005100, a *deficient* number is a number whose proper divisors sum up to the extent smaller than the number itself. First 6 deficient numbers are 1, 2, 3, 4, 5, 7

Usage

```
Deficient(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

```
Abundant, Perfect
```

Examples

```
## generate first 30 Deficient numbers
print(Deficient(30))
```

Equidigital

Equidigital numbers

Description

Under OEIS A046758, an *Equidigital* number has equal digits as the number of digits in its prime factorization including exponents. First 6 Equidigital numbers are 1, 2, 3, 5, 7, 10. Though it doesn't matter which base we use, here we adopt only a base of 10.

```
Equidigital(n, gmp = TRUE)
```

8 Evil

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

```
Frugal, Extravagant
```

Examples

```
## generate first 20 Equidigital numbers
print(Equidigital(20))
```

Evil

Evil numbers

Description

Under OEIS A001969, an *Evil* number has an even number of 1's in its binary expansion. First 6 Evil numbers are 0, 3, 5, 6, 9, 10.

Usage

```
Evil(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

Odious

```
## generate first 20 Evil numbers
print(Evil(20))
```

Extravagant 9

Extravagant

Extravagant numbers

Description

Under OEIS A046760, an *Extravagant* number has less digits than the number of digits in its prime factorization including exponents. First 6 Extravagant numbers are 4, 6, 8, 9, 12, 18. Though it doesn't matter which base we use, here we adopt only a base of 10.

Usage

```
Extravagant(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

```
Frugal, Equidigital
```

Examples

```
## generate first 20 Extravagant numbers
print(Extravagant(20))
```

Factorial

Factorial numbers

Description

Under OEIS A000142, a *Factorial* is the product of all positive integers smaller than or equal to the number. First 6 such numbers are 1, 1, 2, 6, 24, 120

```
Factorial(n, gmp = TRUE)
```

10 Factorial.Alternating

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 10 Factorials
print(Factorial(10))
```

Factorial. Alternating Alternating Factorial numbers

Description

Under OEIS A005165, an *Alternating Factorial* is the absolute value of the alternating sum of the first n factorials of positive integers. First 6 such numbers are 0, 1, 1, 5, 19, 101.

Usage

```
Factorial.Alternating(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

Factorial

```
## generate first 5 Alternating Factorial numbers
print(Factorial.Alternating(5))
```

Factorial.Double 11

Factorial.Double

Double Factorial numbers

Description

Under OEIS A000165 and A001147, a *Double Factorial* is the factorial of numbers with same parity. For example, if n = 5, then n!! = 5 * 3 * 1.

Usage

```
Factorial.Double(n, gmp = TRUE, odd = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

odd a logical; TRUE for double factorial of odd numbers, FALSE for even numbers.

Value

a vector of length n containing first entries from the sequence.

See Also

Factorial

Examples

```
## generate first 10 double factorials
print(Factorial.Double(10))
```

Fibonacci

Fibonacci numbers

Description

Under OEIS A000045, the nth Fibonnaci number is given as

$$F_n = F_{n-1} + F_{n-2}$$

where the first 6 entries are 0, 1, 1, 2, 3, 5 with $n \ge 0$.

12 Frugal

Usage

```
Fibonacci(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise (default:

TRUE).

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 30 Fibonacci numbers
print(Fibonacci(30))
```

Frugal

Frugal numbers

Description

Under OEIS A046759, a *Frugal* number has more digits than the number of digits in its prime factorization including exponents. First 6 Frugal numbers are 125, 128, 243, 256, 343, 512. Though it doesn't matter which base we use, here we adopt only a base of 10.

Usage

```
Frugal(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

```
Extravagant, Equidigital
```

Happy 13

Examples

```
## generate first 5 Frugal numbers
print(Frugal(5))
```

Нарру

Happy numbers

Description

Under OEIS A007770, a *Happy* number is defined by the process that starts from arbitrary positive integer and replaces the number by the sum of the squares of each digit until the number is 1. First 6 Happy numbers are 1, 7, 10, 13, 19, 23.

Usage

```
Happy(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 30 happy numbers
print(Happy(30))
```

Juggler

Juggler sequence

Description

Under OEIS A094683, a Juggler sequence is an integer-valued sequence that starts with a nonnegative number iteratively follows that $J_{k+1} = floor(J_k^{1/2})$ if J_k is even, or $J_{k+1} = floor(J_k^{3/2})$ if odd. No first 6 terms are given since it all depends on the starting value.

```
Juggler(start, gmp = TRUE)
```

Juggler.Largest

Arguments

start the starting nonnegative integer.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector recording the sequence of unknown length a priori.

Examples

```
## let's start from 9 and show the sequence
print(Juggler(9))
```

Juggler.Largest

Largest value for Juggler sequence

Description

Under OEIS A094716, the *Largest value for Juggler sequence* is the largest value in trajectory of a sequence that starts from n. First 6 terms are 0, 1, 2, 36, 4, 36 that n starting from 0 is conventional choice.

Usage

```
Juggler.Largest(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

Juggler

```
## generate first 10 numbers of largest values for Juggler sequences
print(Juggler.Largest(10))
```

Juggler.Nsteps 15

Juggler.Nsteps

Number of steps for Juggler sequence

Description

Under OEIS A007320, a Number of steps for Juggler sequence literally counts the number of steps required for a sequence that starts from n. First 6 terms are 0, 1, 6, 2, 5, 2 that n starting from 0 is conventional choice. Note that when it counts *number of steps*, not the length of the sequence including the last 1.

Usage

```
Juggler.Nsteps(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

Juggler

Examples

```
## generate first 10 numbers of steps for Juggler sequences
print(Juggler.Nsteps(10))
```

Lucas

Lucas numbers

Description

Under OEIS A000032, the nth Lucas number is given as

$$F_n = F_{n-1} + F_{n-2}$$

where the first 6 entries are 2, 1, 3, 4, 7, 11.

```
Lucas(n, gmp = TRUE)
```

16 Motzkin

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

Fibonacci

Examples

```
## generate first 30 Lucas numbers
print(Lucas(30))
```

Motzkin

Motzkin numbers

Description

Under OEIS A001006, a *Motzkin* number for a given n is the number of ways for drawing non-intersecting chords among n points on a circle, where the first 7 entries are 1, 1, 2, 4, 9, 21, 51.

Usage

```
Motzkin(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

```
## generate first 30 Motzkin numbers
print(Motzkin(30))
```

Odious 17

Odious

Odious numbers

Description

Under OEIS A000069, an *Odious* number has an odd number of 1's in its binary expansion. First 6 Odious numbers are 1, 2, 4, 7, 8, 11.

Usage

```
Odious(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

See Also

Evil

Examples

```
## generate first 20 Odious numbers
print(Odious(20))
```

Padovan

Padovan numbers

Description

Under OEIS A000931, the nth Padovan number is given as

$$F_n = F_{n-2} + F_{n-3}$$

where the first 6 entries are 1, 0, 0, 1, 0, 1.

```
Padovan(n, gmp = TRUE)
```

Palindromic Palindromic

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 30 Padovan numbers
print(Padovan(30))
```

Palindromic

Palindromic numbers

Description

Under OEIS A002113, a *Palindromic* number is a number that remains the same when its digits are reversed. First 6 Palindromic numbers in decimal are 0, 1, 2, 3, 4, 5. This function supports various base by specifying the parameter base but returns are still represented in decimal.

Usage

```
Palindromic(n, base = 10, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

base choice of base.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

```
## generate first 30 palindromic number in decimal
print(Palindromic(30))
```

Palindromic.Squares 19

Palindromic. Squares Palindromic squares

Description

Under OEIS A002779, a *Palindromic square* is a number that is both Palindromic and Square. First 6 such numbers are 0, 1, 4, 9, 121, 484. It uses only the base 10 decimals.

Usage

```
Palindromic.Squares(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 10 palindromic squares
print(Palindromic.Squares(10))
```

Perfect

Perfect numbers

Description

Under OEIS A000396, a *Perfect* number is a number whose proper divisors sum up to the extent equal to the number itself. First 6 abundant numbers are 6, 28, 496, 8128, 33550336, 8589869056.

Usage

```
Perfect(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

20 Perrin

Value

a vector of length n containing first entries from the sequence.

See Also

```
Deficient, Abundant
```

Examples

```
## Not run:
## generate first 7 Perfect numbers
print(Perfect(10))
## End(Not run)
```

Perrin

Perrin numbers

Description

Under OEIS A001608, the nth Perrin number is given as

$$F_n = F_{n-2} + F_{n-3}$$

where the first 6 entries are 3, 0, 2, 3, 2, 5.

Usage

```
Perrin(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

```
## generate first 30 Perrin numbers
print(Perrin(30))
```

Powerful 21

Powerful

Powerful numbers

Description

Under OEIS A001694, a *Powerful* number is a positive integer such that for every prime p dividing the number, p^2 also divides the number. First 6 powerful numbers are 1, 4, 8, 9, 16, 25.

Usage

```
Powerful(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 20 Powerful numbers
print(Powerful(20))
```

Prime

Prime numbers

Description

Under OEIS A000040, a *Prime* number is a natural number with no positive divisors other than 1 and itself. First 6 prime numbers are 2, 3, 5, 7, 11, 13.

Usage

```
Prime(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Square Square

Examples

```
## generate first 30 Regular numbers
print(Prime(30))
```

Regular

Regular numbers

Description

Under OEIS A051037, a *Regular* number - also known as 5-smooth - is a positive integer that even divide powers of 60, or equivalently, whose prime divisors are only 2,3, and 5. First 6 Regular numbers are 1, 2, 3, 4, 5, 6.

Usage

```
Regular(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 20 Regular numbers
print(Regular(20))
```

Square

Square numbers

Description

Under OEIS A000290, a Square number is

$$A_n = n^2$$

for $n \ge 0$. First 6 Square numbers are 0, 1, 4, 9, 16, 25.

```
Square(n, gmp = TRUE)
```

Squarefree 23

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 20 Square numbers
print(Square(20))
```

Squarefree

Squarefree numbers

Description

Under OEIS A005117, a *Squarefree* number is a number that are not divisible by a square of a smaller integer greater than 1. First 6 Squarefree numbers are 1, 2, 3, 5, 6, 7.

Usage

```
Squarefree(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

```
## generate first 30 Squarefree numbers
print(Squarefree(30))
```

24 Thabit

Telephone

Telephone numbers

Description

Under OEIS A000085, a *Telephone* number - also known as *Involution* number - is counting the number of connection patterns in a telephone system with n subscribers, or in a more mathematical term, the number of self-inverse permutations on n letters. First 6 Telephone numbers are 1, 1, 2, 4, 10, 26,

Usage

```
Telephone(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 20 Regular numbers
print(Telephone(20))
```

Thabit

Thabit numbers

Description

Under OEIS A055010, the nth Thabit number is given as

$$A_n = 3 * 2^{n-1} - 1$$

where the first 6 entries are 0, 2, 5, 11, 23, 47 with $A_0 = 0$.

```
Thabit(n, gmp = TRUE)
```

Triangular 25

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

Examples

```
## generate first 30 Thabit numbers
print(Thabit(30))
```

Triangular

Triangular numbers

Description

Under OEIS A000217, a *Triangular* number counts objects arranged in an equilateral triangle. First 6 Triangular numbers are 0, 1, 3, 6, 10, 15.

Usage

```
Triangular(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

```
## generate first 20 Triangular numbers
print(Triangular(20))
```

26 Unusual

Unusual

Unusual numbers

Description

Under OEIS A064052, an *Unusual* number is a natural number whose largest prime factor is strictly greater than square root of the number. First 6 Unusual numbers are 2, 3, 5, 6, 7, 10.

Usage

```
Unusual(n, gmp = TRUE)
```

Arguments

n the number of first n entries from the sequence.

gmp a logical; TRUE to use large number representation, FALSE otherwise.

Value

a vector of length n containing first entries from the sequence.

```
## generate first 20 Unusual numbers
print(Unusual(20))
```

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