## Package 'FuzzyLP'

August 21, 2023

Title Fuzzy Linear Programming

Type Package

**Description** Provides methods to solve Fuzzy Linear Programming Problems with fuzzy constraints (following different approaches proposed by Verdegay, Zimmermann, Werners and Tanaka), fuzzy costs, and fuzzy technological matrix.

Version 0.1-7

Date 2023-08-19

**License** GPL (>= 3)

ByteCompile TRUE

Imports ROI, FuzzyNumbers, ROI.plugin.glpk

URL https://github.com/olbapjose/FuzzyLP

Suggests R.rsp

VignetteBuilder R.rsp

RoxygenNote 7.2.3

NeedsCompilation no

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**Repository** CRAN

Date/Publication 2023-08-20 22:42:38 UTC

## **R** topics documented:

crispLP
FCLP.classicObjective
FCLP.fixedBeta
FOLP.multiObj
FOLP.ordFun
FOLP.posib
FuzzyLP
GFLP 15

## Index

crispLP

## Description

crispLP use the classic solver (simplex) to solve a crisp linear programming problem:

```
Max f(x) \text{ or } Min f(x)s.t.: Ax <= b
```

## Usage

```
crispLP(objective, A, dir, b, maximum = TRUE, verbose = TRUE)
```

## Arguments

objective	A vector $(c_1, c_2,, c_n)$ with the objective function coefficients $f(x) = c_1 x_1 + + c_n x_n$ .
A	Technological matrix of Real Numbers.
dir	Vector of strings with the direction of the inequalities, of the same length as b. Each element of the vector must be one of "=", ">=", "<=", "<" or ">".
b	Vector with the right hand side of the constraints.
maximum	TRUE to maximize the objective function, FALSE to minimize the objective function.
verbose	TRUE to show aditional screen info, FALSE to hide aditional screen info.

## Value

crispLP returns the solution if the solver has found it or NULL if not.

FCLP.classicObjective Solves a Fuzzy Linear Programming problem with fuzzy constraints trying to assure a minimum (maximum) value of the objective function.

## Description

The goal is to solve a linear programming problem having fuzzy constraints trying to assure a minimum (or maximum) value of the objective function.

$$Max f(x) \text{ or } Min f(x)$$
  
s.t.: 
$$Ax \le b + (1 - \beta) * t$$

Where t means we allow not to satisfy the constraint, exceeding the bound b at most in t.

FCLP.classicObjective solves the problem trying to assure a minimum (maximum) value  $z_0$  of the objective function ( $f(x) \ge z_0$  in maximization problems,  $f(x) \le z_0$  in minimization problems).

FCLP.fuzzyObjective solves the problem trying to assure a minimum (maximum) value  $z_0$  of the objective function with tolerance  $t_0$  ( $f(x) \ge z_0 - (1 - \beta)t_0$  in maximization problems,  $f(x) \le z_0 + (1 - \beta)t_0$  in minimization problems).

FCLP.fuzzyUndefinedObjective solves the problem trying to assure a minimum (maximum) value of the objective function with tolerance but the user doesn't fix the bound nor the tolerance. The function estimate a bound and a tolerance and call FCLP.fuzzyObjective using them.

FCLP.fuzzyUndefinedNormObjective solves the problem trying to assure a minimum (maximum) value of the objective function with tolerance but the user doesn't fix the bound nor the tolerance. The function normalize the objective, estimate a bound and a tolerance and call FCLP.fuzzyObjective using them.

#### Usage

```
FCLP.classicObjective(
   objective,
   A,
   dir,
   b,
   t,
   z0 = 0,
   maximum = TRUE,
   verbose = TRUE
)
FCLP.fuzzyObjective(
   objective,
   A,
   dir,
   b,
```

```
t,
  z0 = 0,
  t0 = 0,
 maximum = TRUE,
 verbose = TRUE
)
FCLP.fuzzyUndefinedObjective(
  objective,
 Α,
  dir,
 b,
  t,
 maximum = TRUE,
  verbose = TRUE
)
FCLP.fuzzyUndefinedNormObjective(
  objective,
 Α,
 dir,
 b,
  t,
 maximum = TRUE,
  verbose = TRUE
```

```
)
```

## Arguments

objective	A vector $(c_1, c_2, \ldots, c_n)$ with the objective function coefficients $f(x) = c_1 x_1 + c_2 x_2 + c_2 x_1 + c_2 x_2 + c_2 x_$
	$\ldots + c_n x_n.$
А	Technological matrix of Real Numbers.
dir	Vector of strings with the direction of the inequalities, of the same length as b and t. Each element of the vector must be one of "=", ">=", "<=", "<" or ">".
b	Vector with the right hand side of the constraints.
t	Vector with the tolerance of each constraint.
z0	The minimum (maximum in a minimization problem) value of the objective function to reach. Only used in FCLP.classicObjective and FCLP.fuzzyObjective
maximum	TRUE to maximize the objective function, FALSE to minimize the objective func- tion.
verbose	TRUE to show aditional screen info, FALSE to hide aditional screen info.
tØ	The tolerance value to the minimum (or maximum) bound for the objective func- tion. Only used in FCLP.fuzzy0bjective.

## Value

FCLP.classicObjective returns a solution reaching the given minimum (maximum) value of the objective function if the solver has found it (trying to maximize  $\beta$ ) or NULL if not. Note that the

4

#### FCLP.classicObjective

found solution may not be the optimum for the  $\beta$  returned, trying  $\beta$  in FCLP.fixedBeta may obtain better results.

FCLP.fuzzyObjective returns a solution reaching the given minimum (maximum) value of the objective function if the solver has found it (trying to maximize  $\beta$ ) or NULL if not. Note that the found solution may not be the optimum for the  $\beta$  returned, trying  $\beta$  in FCLP.fixedBeta may obtain better results.

FCLP.fuzzyUndefinedObjective returns a solution reaching the estimated minimum (maximum) value of the objective function if the solver has found it (trying to maximize  $\beta$ ) or NULL if not.

FCLP.fuzzyUndefinedNormObjective returns a solution reaching the estimated minimum (maximum) value of the objective function if the solver has found it (trying to maximize  $\beta$ ) or NULL if not.

#### References

Zimmermann, H. Description and optimization of fuzzy systems. International Journal of General Systems, 2:209-215, 1976.

Werners, B. An interactive fuzzy programming system. Fuzzy Sets and Systems, 23:131-147, 1987.

Tanaka, H. and Okuda, T. and Asai, K. On fuzzy mathematical programming. Journal of Cybernetics, 3,4:37-46, 1974.

#### See Also

FCLP.fixedBeta, FCLP.sampledBeta

```
## maximize: 3*x1 + x2 >= z0
             1.875*x1 - 1.5*x2 <= 4 + (1-beta)*5
## s.t.:
##
               4.75*x1 + 2.125*x2 <= 14.5 + (1-beta)*6
##
                x1, x2 are non-negative real numbers
obj <- c(3, 1)
A \le matrix(c(1.875, 4.75, -1.5, 2.125), nrow = 2)
dir <- c("<=", "<=")
b <- c(4, 14.5)
t <- c(5, 6)
max <- TRUE
# Problem with solution
FCLP.classicObjective(obj, A, dir, b, t, z0=11, maximum=max, verbose = TRUE)
# This problem has a bound impossible to reach
FCLP.classicObjective(obj, A, dir, b, t, z0=14, maximum=max, verbose = TRUE)
# This problem has a fuzzy bound impossible to reach
FCLP.fuzzyObjective(obj, A, dir, b, t, z0=14, t0=1, maximum=max, verbose = TRUE)
# This problem has a fuzzy bound reachable
FCLP.fuzzyObjective(obj, A, dir, b, t, z0=14, t0=2, maximum=max, verbose = TRUE)
```

```
# We want the function estimates a bound and a tolerance
FCLP.fuzzyUndefinedObjective(obj, A, dir, b, t, maximum=max, verbose = TRUE)
```

```
# We want the function estimates a bound and a tolerance
FCLP.fuzzyUndefinedNormObjective(obj, A, dir, b, t, maximum=max, verbose = TRUE)
```

FCLP.fixedBeta Solves a Fuzzy Linear Programming problem with fuzzy constraints.

## Description

The goal is to solve a linear programming problem having fuzzy constraints.

$$Max f(x) \text{ or } Min f(x)$$

s.t.:  $Ax \le b + (1 - \beta) * t$ 

Where t means we allow not to satisfy the constraint, exceeding the bound b at most in t.

FCLP.fixedBeta uses the classic solver (simplex) to solve the problem with a fixed value of  $\beta$ .

FCLP.sampledBeta solves the problem in the same way than FCLP.fixedBeta but using several  $\beta's$  taking values in a sample of the [0, 1] inteval.

## Usage

```
FCLP.fixedBeta(
  objective,
  Α,
  dir.
  b,
  t,
  beta = 0.5,
 maximum = TRUE,
  verbose = TRUE
)
FCLP.sampledBeta(
  objective,
  Α,
  dir.
  b,
  t,
  min = 0,
  max = 1,
  step = 0.25,
```

```
maximum = TRUE,
verbose = TRUE
)
```

#### Arguments

objective	A vector $(c_1, c_2, \ldots, c_n)$ with the objective function coefficients $f(x) = c_1 x_1 + \ldots + c_n x_n$ .
A	Technological matrix of Real Numbers.
dir	Vector of strings with the direction of the inequalities, of the same length as b and t. Each element of the vector must be one of "=", ">=", "<=", "<" or ">".
b	Vector with the right hand side of the constraints.
t	Vector with the tolerance of each constraint.
beta	The value of $\beta$ to be used.
maximum	TRUE to maximize the objective function, $FALSE$ to minimize the objective function.
verbose	TRUE to show aditional screen info, FALSE to hide aditional screen info.
min	The lower bound of the interval to take the sample.
max	The upper bound of the interval to take the sample.
step	The sampling step.

## Value

FCLP.fixedBeta returns the solution for the given beta if the solver has found it or NULL if not.

FCLP.sampledBeta returns the solutions for the sampled  $\beta's$  if the solver has found them. If the solver hasn't found solutions for any of the  $\beta's$  sampled, return NULL.

## References

Verdegay, J.L. Fuzzy mathematical programming. In: Fuzzy Information and Decision Processes, pages 231-237, 1982. M.M. Gupta and E.Sanchez (eds).

Delgado, M. and Herrera, F. and Verdegay, J.L. and Vila, M.A. Post-optimality analisys on the membership function of a fuzzy linear programming problem. Fuzzy Sets and Systems, 53:289-297, 1993.

## See Also

FCLP.classicObjective, FCLP.fuzzyObjective

FCLP.fuzzyUndefinedObjective,FCLP.fuzzyUndefinedNormObjective

#### Examples

```
## maximize: 3*x1 + x2
                          - 1.5*x2 <= 4 + (1-beta)*5
## s.t.:
              1.875*x1
##
                4.75*x1 + 2.125*x2 <= 14.5 + (1-beta)*6
##
                 x1, x2 are non-negative real numbers
obj <- c(3, 1)
A \leftarrow matrix(c(1.875, 4.75, -1.5, 2.125), nrow = 2)
dir <- c("<=", "<=")
b <- c(4, 14.5)
t <- c(5, 6)
valbeta <- 0.5
max <- TRUE
FCLP.fixedBeta(obj, A, dir, b, t, beta=valbeta, maximum = max, verbose = TRUE)
FCLP.sampledBeta(obj, A, dir, b, t, min=0, max=1, step=0.25, maximum = max, verbose = TRUE)
```

FOLP.multiObj	Solves a fuzzy objective linear programming problem using Represen-
	tation Theorem.

#### Description

The goal is to solve a linear programming problem having Trapezoidal Fuzzy Numbers as coefficients in the objective function  $(f(x) = c_1^f x_1 + \ldots + c_n^f x_n)$ .

Max f(x) or Min f(x) $s.t.: \quad Ax <= b$ 

FOLP.multiObj uses a multiobjective approach. This approach is based on each  $\beta$ -cut of a Trapezoidal Fuzzy Number is an interval (different for each  $\beta$ ). So the problem may be considered as a Parametric Linear Problem. For a value of  $\beta$  fixed, the problem becomes a Multiobjective Linear Problem, this problem may be solved from different approachs, FOLP.multiObj solves it using weights, the same weight for each objective.

FOLP. interv uses an intervalar approach. This approach is based on each  $\beta$ -cut of a Trapezoidal Fuzzy Number is an interval (different for each  $\beta$ ). Fixing an  $\beta$ , using interval arithmetic and defining an order relation for intervals is possible to compare intervals, this transforms the problem in a biobjective problem (involving the minimum and the center of intervals). Finally FOLP.interv use weights to solve the biobjective problem.

FOLP.strat uses a stratified approach. This approach is based on that  $\beta$ -cuts are a sequence of nested intervals. Fixing an  $\beta$  two auxiliary problems are solved, the first replacing the fuzzy coefficients by the lower limits of the  $\beta$ -cuts, the second doing the same with the upper limits. The results of the two auxiliary problems allows to formulate a new auxiliary problem, this problem tries to maximize a parameter  $\lambda$ .

8

## Usage

```
FOLP.multiObj(
 objective,
 Α,
 dir,
 b,
 maximum = TRUE,
 min = 0,
 max = 1,
 step = 0.25
)
FOLP.interv(
  objective,
 Α,
 dir,
 b,
 maximum = TRUE,
 w1 = 0.5,
 min = 0,
 max = 1,
  step = 0.25
)
```

FOLP.strat(objective, A, dir, b, maximum = TRUE, min = 0, max = 1, step = 0.25)

## Arguments

objective	A vector $(c_1^f, c_2^f,, c_n^f)$ of Trapezoidal Fuzzy Numbers with the objective function coefficients $f(x) = c_1^f x_1 + + c_n^f x_n$ . Note that any of the coefficients may also be Real Numbers.
A	Technological matrix of Real Numbers.
dir	Vector of strings with the direction of the inequalities, of the same length as b. Each element of the vector must be one of "=", ">=", "<=", "<" or ">".
b	Vector with the right hand side of the constraints.
maximum	TRUE to maximize the objective function, FALSE to minimize the objective function.
min	The lower bound of the interval to take the sample.
max	The upper bound of the interval to take the sample.
step	The sampling step.
w1	Weight to be used, w2 is calculated as w2=1-w1. w1 must be in the interval $[0, 1]$ . Only used in FOLP.interv.

## Value

FOLP.multiObj returns the solutions for the sampled  $\beta's$  if the solver has found them. If the solver hasn't found solutions for any of the  $\beta's$  sampled, return NULL.

FOLP.interv returns the solutions for the sampled  $\beta's$  if the solver has found them. If the solver hasn't found solutions for any of the  $\beta's$  sampled, return NULL.

FOLP.strat returns the solutions and the value of  $\lambda$  for the sampled  $\beta's$  if the solver has found them. If the solver hasn't found solutions for any of the  $\beta's$  sampled, return NULL. A greater value of  $\lambda$  may be interpreted as the obtained solution is better.

#### References

Verdegay, J.L. Fuzzy mathematical programming. In: Fuzzy Information and Decision Processes, pages 231-237, 1982. M.M. Gupta and E.Sanchez (eds).

Delgado, M. and Verdegay, J.L. and Vila, M.A. Imprecise costs in mathematical programming problems. Control and Cybernetics, 16 (2):113-121, 1987.

Bitran, G.. Linear multiple objective problems with interval coefficients. Management Science, 26(7):694-706, 1985.

Alefeld, G. and Herzberger, J. Introduction to interval computation. 1984.

Moore, R. Method and applications of interval analysis, volume 2. SIAM, 1979.

Rommelfanger, H. and Hanuscheck, R. and Wolf, J. Linear programming with fuzzy objectives. Fuzzy Sets and Systems, 29:31-48, 1989.

## See Also

FOLP.ordFun, FOLP.posib

```
## maximize: [0,2,3]*x1 + [1,3,4,5]*x2
## s.t.:
             x1 + 3*x2 <= 6
##
                x1 + x2 <= 4
                x1, x2 are non-negative real numbers
##
obj <- c(FuzzyNumbers::TrapezoidalFuzzyNumber(0,2,2,3),</pre>
         FuzzyNumbers::TrapezoidalFuzzyNumber(1,3,4,5))
A<-matrix(c(1, 1, 3, 1), nrow = 2)
dir <- c("<=", "<=")
b <- c(6, 4)
max <- TRUE
# Using a Multiobjective approach.
FOLP.multiObj(obj, A, dir, b, maximum = max, min=0, max=1, step=0.2)
# Using a Intervalar approach.
FOLP.interv(obj, A, dir, b, maximum = max, w1=0.3, min=0, max=1, step=0.2)
# Using a Stratified approach.
FOLP.strat(obj, A, dir, b, maximum = max, min=0, max=1, step=0.2)
```

FOLP.ordFun

Solves a fuzzy objective linear programming problem using ordering functions.

## Description

The goal is to solve a linear programming problem having Trapezoidal Fuzzy Numbers as coefficients in the objective function  $(f(x) = c_1^f x_1 + \ldots + c_n^f x_n)$ .

```
Max f(x) \text{ or } Min f(x)s.t.: Ax <= b
```

FOLP.ordFun uses ordering functions to compare Fuzzy Numbers.

## Usage

```
FOLP.ordFun(
   objective,
   A,
   dir,
   b,
   maximum = TRUE,
   ordf = c("Yager1", "Yager3", "Adamo", "Average", "Custom"),
   ...,
   FUN = NULL
)
```

## Arguments

objective	A vector $(c_1^f, c_2^f,, c_n^f)$ of Trapezoidal Fuzzy Numbers with the objective function coefficients $f(x) = c_1^f x_1 + + c_n^f x_n$ . Note that any of the coefficients may also be Real Numbers.
A	Technological matrix of Real Numbers.
dir	Vector of strings with the direction of the inequalities, of the same length as b. Each element of the vector must be one of "=", ">=", "<=", "<" or ">".
b	Vector with the right hand side of the constraints.
maximum	TRUE to maximize the objective function, $FALSE$ to minimize the objective function.
ordf	Ordering function to be used, ordf must be one of "Yager1", "Yager3", "Adamo", "Average" or "Custom". The "Custom" option allows to use a custom linear ordering function that must be placed as FUN argument. If a non linear function is used the solution may not be optimal.
	Additional parameters to the ordering function if needed.
	• Yager1 doesn't need any parameters.

	<ul> <li>Yager3 doesn't need any parameters.</li> </ul>
	• Adamo needs a alpha parameter which must be in the interval [0,1].
	• Average needs two parameters, lambda must be in the interval [0,1] and t that must be greater than 0.
	• If Custom function needs parameters, put them here. Although not required, it is recommended to name the parameters.
FUN	Custom linear ordering function to be used if the value of ordf is "Custom". If any of the coefficients of the objective function are Real Numbers, the user must assure that the function FUN works well not only with Trapezoidal Fuzzy Numbers but also with Real Numbers.

#### Value

FOLP. ordFun returns the solution if the solver has found it or NULL if not.

## References

Gonzalez, A. A studing of the ranking function approach through mean values. Fuzzy Sets and Systems, 35:29-41, 1990.

Cadenas, J.M. and Verdegay, J.L. Using Fuzzy Numbers in Linear Programming. IEEE Transactions on Systems, Man, and Cybernetics-Part B: Cybernetics, vol. 27, No. 6, December 1997.

Tanaka, H., Ichihashi, H. and Asai, F. A formulation of fuzzy linear programming problems based a comparison of fuzzy numbers. Control and Cybernetics, 13:185-194, 1984.

#### See Also

FOLP.multiObj, FOLP.interv, FOLP.strat, FOLP.posib

```
## maximize: [0,2,3]*x1 + [1,3,4,5]*x2
## s.t.:
                x1 + 3*x2 <= 6
##
                x1 + x2 <= 4
##
               x1, x2 are non-negative real numbers
obj <- c(FuzzyNumbers::TrapezoidalFuzzyNumber(0,2,2,3),</pre>
        FuzzyNumbers::TrapezoidalFuzzyNumber(1,3,4,5))
A<-matrix(c(1, 1, 3, 1), nrow = 2)
dir <- c("<=", "<=")
b <- c(6, 4)
max <- TRUE
FOLP.ordFun(obj, A, dir, b, maximum = max, ordf="Yager1")
FOLP.ordFun(obj, A, dir, b, maximum = max, ordf="Yager3")
FOLP.ordFun(obj, A, dir, b, maximum = max, ordf="Adamo", 0.5)
FOLP.ordFun(obj, A, dir, b, maximum = max, ordf="Average", lambda=0.8, t=3)
# Define a custom linear function
av <- function(tfn) {mean(FuzzyNumbers::core(tfn))}</pre>
FOLP.ordFun(obj, A, dir, b, maximum = max, ordf="Custom", FUN=av)
```

```
# Define a custom linear function
avp <- function(tfn, a) {a*mean(FuzzyNumbers::core(tfn))}
FOLP.ordFun(obj, A, dir, b, maximum = max, ordf="Custom", FUN=avp, a=2)
```

```
FOLP.posib
```

Solves a fuzzy objective linear programming problem using Representation Theorem.

#### Description

The goal is to solve a linear programming problem having Trapezoidal Fuzzy Numbers as coefficients in the objective function  $(f(x) = c_1^f x_1 + \ldots + c_n^f x_n)$ .

 $\begin{aligned} Max\,f(x)\;or\;Min\;f(x)\\ s.t.:\quad Ax<=b \end{aligned}$ 

FOLP.posib uses a possibilistic approach. This approach is based on Trapezoidal Fuzzy Numbers arithmetic, so the whole objective may be considered as a Fuzzy Number itself. Defining a notion of maximum for this kind of numbers (a weighted average of the minimum and maximum of the support of the Trapezoidal number).

## Usage

```
FOLP.posib(objective, A, dir, b, maximum = TRUE, w1 = 0.5)
```

#### Arguments

objective	A vector $(c_1^f, c_2^f,, c_n^f)$ of Trapezoidal Fuzzy Numbers with the objective function coefficients $f(x) = c_1^f x_1 + + c_n^f x_n$ . Note that any of the coefficients may also be Real Numbers.
A	Technological matrix of Real Numbers.
dir	Vector of strings with the direction of the inequalities, of the same length as b. Each element of the vector must be one of "=", ">=", "<=", "<" or ">".
b	Vector with the right hand side of the constraints.
maximum	TRUE to maximize the objective function, FALSE to minimize the objective function.
w1	Weight to be used, w2 is calculated as w2=1-w1. w1 must be in the interval $[0, 1]$ .

## Value

FOLP. posib returns the solution for the given weights if the solver has found it or NULL if not.

#### References

Dubois, D. and Prade, H. Operations in fuzzy numbers. International Journal of Systems Science, 9:613-626, 1978.

## See Also

```
FOLP.ordFun, FOLP.multiObj, FOLP.interv, FOLP.strat
```

#### Examples

FuzzyLP

Fuzzy Linear Programming

#### Description

FuzzyLP is a package to solve fuzzy linear programming problems.

## Details

FuzzyLP implements several algorithms for solving fuzzy linear programming

#### References

Villacorta, P.J., Rabelo, C.A., Pelta, D.A., and Verdegay, J.L. FuzzyLP: An R Package for Solving Fuzzy Linear Programming Problems. In: Kacprzyk J., Filev D., Beliakov G. (eds) Granular, Soft and Fuzzy Approaches for Intelligent Systems:209-230. Springer, 2017.

Cadenas, J.M. and Verdegay, J.L. PROBO: an interactive system in fuzzy linear programming. Fuzzy Sets and Systems 76(3):319-332, 1995.

Cadenas, J.M. and Verdegay, J.L. Modelos de Optimizacion con Datos Imprecisos. Servicio de Publicaciones, Universidad de Murcia, 1999.

Bellman, R. and Zadeh, L. Decision making in a fuzzy environment. Management Science 17 (B) 4:141-164, 1970.

14

GFLP

Solves a maximization (minimization) problem having fuzzy coefficients in the constraints, the objective function and/or the technological matrix.

## Description

The goal is to solve a linear programming problem having Trapezoidal Fuzzy Numbers as coefficients in the constraints, the objective function and/or the technological matrix.

```
\begin{aligned} &Max\,f(x)\ or\ Min\ f(x)\\ &s.t.:\quad \widetilde{A}x<=\widetilde{b}+(1-\beta)*\widetilde{t} \end{aligned}
```

This function uses different ordering functions for the objective function and for the constraints.

## Usage

```
GFLP(
   objective,
   A,
   dir,
   b,
   t,
   maximum = TRUE,
   ordf_obj = c("Yager1", "Yager3", "Adamo", "Average"),
   ordf_obj_param = NULL,
   ordf_res = c("Yager1", "Yager3", "Adamo", "Average"),
   ordf_res_param = NULL,
   min = 0,
   max = 1,
   step = 0.25
)
```

## Arguments

objective	A vector $(c_1^f, c_2^f,, c_n^f)$ of Trapezoidal Fuzzy Numbers with the objective function coefficients $f(x) = c_1^f x_1 + + c_n^f x_n$ . Note that any of the coefficients may also be Real Numbers.
A	Technological matrix containing Trapezoidal Fuzzy Numbers and/or Real Numbers.
dir	Vector of strings with the direction of the inequalities, of the same length as b and t. Each element of the vector must be one of "=", ">=", "<=", "<" or ">".
b	Vector with the right hand side of the constraints. b may contain Trapezoidal Fuzzy Numbers and/or Real Numbers.
t	Vector with the tolerance of each constraint. t may contain Trapezoidal Fuzzy Numbers and/or Real Numbers.

maximum	TRUE to maximize the objective function, FALSE to minimize the objective func- tion.
ordf_obj	Ordering function to be used in the objective function, ordf_obj must be one of "Yager1", "Yager3", "Adamo" or "Average".
ordf_obj_param	Parameters need by ordf_obj function, if it needs more than one parameter, use a named vector. See FOLP.ordFun for more information about the ordering functions parameters.
ordf_res	Ordering function to be used in the constraints, ordf_res must be one of "Yager1", "Yager3", "Adamo" or "Average".
ordf_res_param	Parameters need by ordf_res function, if it needs more than one parameter, use a named vector. See FOLP.ordFun for more information about the ordering functions parameters.
min	The lower bound of the interval to take the sample.
max	The upper bound of the interval to take the sample.
step	The sampling step.

## Value

GFLP returns the solutions for the sampled  $\beta's$  if the solver has found them. If the solver hasn't found solutions for any of the  $\beta's$  sampled, return NULL.

#### References

Gonzalez, A. A studing of the ranking function approach through mean values. Fuzzy Sets and Systems, 35:29-41, 1990.

Cadenas, J.M. and Verdegay, J.L. Using Fuzzy Numbers in Linear Programming. IEEE Transactions on Systems, Man, and Cybernetics-Part B: Cybernetics, vol. 27, No. 6, December 1997.

Tanaka, H., Ichihashi, H. and Asai, F. A formulation of fuzzy linear programming problems based a comparison of fuzzy numbers. Control and Cybernetics, 13:185-194, 1984.

```
## maximize: [1,3,4,5]*x1 + x2
## s.t.:
               [0,2,3,3.5]*x1 + [0,1,1,4]*x2 <= [2,2,2,3] + (1-beta)*[1,2,2,3]
##
                 [3,5,5,6]*x1 + [1.5,2,2,3]*x2 <= 12
##
                 x1, x2 are non-negative real numbers
obj <- c(FuzzyNumbers::TrapezoidalFuzzyNumber(1,3,4,5), 1)</pre>
all <- FuzzyNumbers::TrapezoidalFuzzyNumber(0,2,2,3.5)
a21 <- FuzzyNumbers::TrapezoidalFuzzyNumber(3,5,5,6)
a12 <- -FuzzyNumbers::TrapezoidalFuzzyNumber(0,1,1,4)
a22 <- FuzzyNumbers::TrapezoidalFuzzyNumber(1.5,2,2,3)
A <- matrix(c(a11, a21, a12, a22), nrow = 2)
dir <- c("<=", "<=")
b<-c(FuzzyNumbers::TrapezoidalFuzzyNumber(2,2,2,3), 12)</pre>
t<-c(FuzzyNumbers::TrapezoidalFuzzyNumber(1,2,2,3),0);</pre>
```

## GFLP

max <- TRUE</pre>

GFLP(obj, A, dir, b, t, maximum = max, ordf\_obj="Yager1", ordf\_res="Yager3")
GFLP(obj, A, dir, b, t, maximum = max, ordf\_obj="Adamo", ordf\_obj\_param=0.5, ordf\_res="Yager3")
GFLP(obj, A, dir, b, t, maximum = max, "Average", ordf\_obj\_param=c(t=3, lambda=0.5),
ordf\_res="Adamo", ordf\_res\_param = 0.5)
GFLP(obj, A, dir, b, t, maximum = max, ordf\_obj="Average", ordf\_obj\_param=c(t=3, lambda=0.8),
ordf\_res="Yager3", min = 0, max = 1, step = 0.2)

# Index

crispLP, 2

FCLP.classicObjective, 3, 7 FCLP.fixedBeta, 5, 6, 6 FCLP.fuzzyObjective, 3, 7 FCLP.fuzzyObjective (FCLP.classicObjective), 3 FCLP.fuzzyUndefinedNormObjective, 7 FCLP.fuzzyUndefinedNormObjective (FCLP.classicObjective), 3 FCLP.fuzzyUndefinedObjective, 7 FCLP.fuzzyUndefinedObjective (FCLP.classicObjective), 3 FCLP.sampledBeta, 5 FCLP.sampledBeta(FCLP.fixedBeta), 6 FOLP.interv, *12*, *14* FOLP.interv (FOLP.multiObj), 8 FOLP.multiObj, 8, 12, 14 FOLP.ordFun, *10*, 11, *14*, *16* FOLP.posib, *10*, *12*, 13 FOLP.strat, 12, 14 FOLP.strat(FOLP.multiObj), 8 FuzzyLP, 14 FuzzyLP-package (FuzzyLP), 14

GFLP, 15